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## Nonbonded Attraction in Methyl Vinyl Ether

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Abstract: A detailed ab-initio investigation of the rotational surface of methyl vinyl ether shows that two stable isomers exist, the more "crowded" cisoid-staggered conformer being the structure of lowest energy. This conformational preference is in agreement with experimental results and can be understood in terms of a nonbonded attractive interactions between the methyl group and the double bond. Furthermore, the methyl rotational barriers in the cisoid and transoid conformations have been computed and their relative magnitudes can be also interpreted in terms of nonbonded interactions.

In our continuing studies of nonbonded interactions, we have investigated the conformational properties of the molecule methyl vinyl ether, H<sub>3</sub>COCH=CH<sub>2</sub>. This particular molecule was selected because it can serve as a prototype for the study of nonbonded attractive interactions and their influence upon molecular conformation. In this paper, the results of ab-initio calculations are reported and compared with experimental data. The computational results, in agreement with experimental evidence,<sup>2</sup> show that the most stable conformation of methyl vinyl ether is the one which a chemist might have dismissed on grounds of being "sterically" unfavorable. Subsequently, it is shown that this conformational preference can be understood in terms of a qualitative MO analysis based upon the ideas developed by one of the authors<sup>3-5</sup> and that these ideas are in full accord with the computational data.

## **Ab-Initio Calculations**

In order to study the conformational properties of methyl vinyl ether two rotational motions have to be investigated (see Figure 1), i.e., rotation around the  $C_1$ -O bond (described here in terms of the torsional angle  $\theta$ ) and rotation around the  $O-C_2$  bond (described in terms of the torsional angle  $\Phi$ ). The zero values of the two torsional angles correspond to the cisoid-eclipsed (CE) conformation. The computations were performed with the GAUSSIAN 70 series of programs<sup>6</sup> at two different levels of sophistication. We first made a detailed study of these two rotational motions with a STO-3G<sup>7</sup> basis set. These computations were carried out for various values of the angle  $\Phi$  ( $\Phi = 0, 45, 90, 120, 135,$ 155, and 180°) and at each  $\Phi$  for various values of the angle  $\theta$  ( $\theta = 0, 30, 60, \text{ and } 100^\circ$ ). At this computational level the following bond angles and bond lengths were kept constant (see Figure 1):  $\angle HC_1H = 109.5^\circ$ ;  $\angle HC_3H = 120^\circ$ ;  $r(C_3-H)$  $= r(C_2-H) = 1.07$  Å; and  $r(C_1-H) = 1.09$  Å. The remaining parameters were first optimized in the TE conformation, where important nonbonded interactions are absent, in the following order: (a)  $\angle OC_2C_3$ ; (b)  $\angle C_1OC_2$ ; (c)  $r(C_2-$ C<sub>3</sub>); (d)  $r(C_2-O)$ ; (e)  $\angle C_2C_3H$ ; and (f)  $r(O-C_1)$ . Furthermore, for the various conformations investigated, the following parameters were reoptimized: (i)  $\angle OC_2C_3$  and

 $\angle C_2OC_1$  for all the conformations with  $\theta = 0$  and  $60^\circ$ ; (ii)  $\angle C_2OC_1$  for all the conformations with  $\theta = 30$  and  $100^\circ$  because  $\angle OC_2C_3$  was found to have, in all cases, almost identical values at  $\theta = 0$  and  $60^\circ$  (in the computations at  $\theta = 30^\circ$  $\angle C_3C_2O$  was kept at the value obtained at  $\theta = 0^\circ$ , while for  $\theta = 100^\circ$  at the value obtained at  $\theta = 60^\circ$ ); (iii)  $r(C_2-O)$ for the conformations with  $\theta = 0^\circ$  (for all the conformations with the same  $\Phi$ ,  $r(C_2-O)$  was kept fixed at the value obtained at  $\theta = 0^\circ$ ).

In order to obtain more accurate estimates of the energy differences of interest, we carried out calculations for the conformations listed in Table I using a 4-31G basis set.<sup>8</sup> In the first stage we used the geometries optimized at the STO-3G level and these results are shown in Table I. In the second stage we reoptimized at the 4-31G level certain geometrical parameters which, on the basis of the STO-3G computations, appear to affect the energy the most, i.e.,  $r(O-C_2)$ ,  $\angle OC_2C_3$ ,  $\angle C_1OC_2$ , and  $\angle H_cC_1O$ . The corresponding values, together with the total energies, are listed in Table II.

The potential energy curves for rotation about the  $O-C_2$ bond, determined at the STO-3G and 4-31G levels, are shown in Figure 2. Here, we report only one curve at the 4-31G level, since the relative energies with and without geometry reoptimization are almost identical. The two curves at the STO-3G and 4-31G levels are very similar and predict that only two stable isomers exist: the CS ( $\Phi = 0^{\circ}$ ) and TS ( $\Phi = 180^{\circ}$ ) conformations. In both cases the planar CS conformer is the most stable isomer. The experimental studies<sup>2</sup> have suggested the existence of two rotamers of methyl vinyl ether with the more stable isomer having a planar cis conformation in accord with the ab initio result. However, there is some disagreement between the theoretical and experimental results about the structure of the less stable rotamer. Electron diffraction data<sup>2c</sup> suggest that it has a nonplanar heavy-atom skeleton with  $\Phi$  in the range 80-110°, while the present computational results indicate a planar transoid form ( $\Phi = 180^{\circ}$ ). It must be emphasized that this latter result has been obtained after a sophisticated geometry optimization. On the other hand, various assumptions were made in the least-squares refinement of the structural

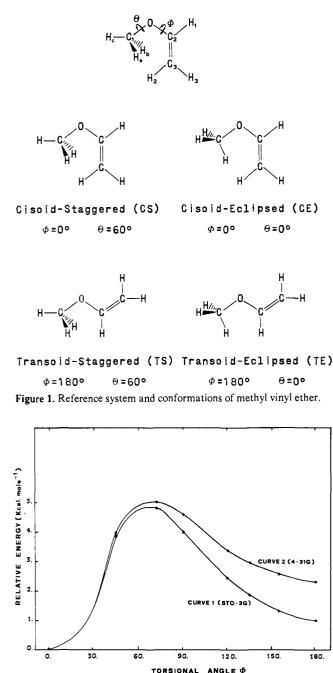


Figure 2. Minimal path for vinyl rotation.

parameters obtained by electron diffraction, the most severe being that the bond angles and bond distances were the same in the two rotamers. The present computations show, instead, that the cisoid rotamer has geometric parameters which differ significantly from those of a second isomer with  $\Phi \ge 90^{\circ}$ . As a result of the present detailed optimization, reasonable values of the various geometric parameters have now become available for various conformations of interest and it seems reasonable to suggest a reexamination of the experimental data. In this connection, it should be pointed out that it is conceivable that the second stable isomer is indeed the one suggested by Owen and Seip<sup>2c</sup> because this geometry is stabilized by a hyperconjugative interaction between the  $\pi$  ethylenic system and the C<sub>1</sub>-O bond.

Table III compares the theoretical and experimental results while the computational details are given in Table IV. It must be noticed again that, while the rotational barrier of the methyl group computed at the STO-3G level agrees

 $(\Phi = 180^\circ, \theta = 60^\circ)$ 4431 b 119.055 53 3950b 91.630 15 89.494 21.992 21.26 -0. 17  $(\Phi = 155^\circ, \theta = 60^\circ)$ 10 57 119.207 77 .4413 .4007 89.494 91.629 22.03 .52 .58 45 21  $(\Phi = 135^{\circ}, \theta = 60^{\circ})$ 189.493 33 191.629 09 119.350 61 .3112 .4042 .4432 21.58 .397 17.10 22.02 0.0222.08  $(\Phi = 120^\circ, \theta = 60^\circ)$ 91.628 44 119.566 21 .4427 4058 89.492 .48/ 2 Geometrical Parameters<sup>a</sup> for Various Conformations of Methyl Vinyl Ether Computed at the STO-3G Level,  $(\Phi=90^\circ, \theta=60^\circ)$ -189.489 87 -191.626 56 119.986 92 .4446 4114 <u>60</u> 69 16.75  $(\Phi = 45^{\circ}, \theta = 49, 47^{\circ}) (\Phi = 72.46^{\circ}, \theta = 60^{\circ})$ 189.488 59 191.625 85 120.385 93 44316 3153b .406021.99b20.00c20.00cTogether with the Corresponding Energies Computed at the STO-3G and 4-31G Levels 189.489 95 191.627 47 120.611 02 .4431*b* 20.00c20.00c21.99b<u>د</u>  $(\Phi = 0^\circ, \theta = 60^\circ)$ 189.496 28 191.633 86 121.181 56 3148 .4371 3.79e 115.49 21.63 29.09 96 Fotal energy (STO-3G) Fotal energy (4-3IG) Nuclear energy filt angle*d* ∠H<sub>2</sub>C<sub>3</sub>E Lable I. ပ်ဝ၃

a Bond lengths in A and angles in deg. b Optimized for the TE conformation at the STO-3G level (see Table III). c Not optimized. a Tilt angle of the local threefold axis of the methyl group to the CO bond. c Tilt angle optimized in the  $H_{cC_{i}O}$  plane (a positive tilt corresponds to a  $H_{cC_{i}O}$  angle > 109.5°). F Tilt angle optimized in the  $H_{aC_{i}O}$  angle > 109.5°).

Table II. Geometrical Parameters<sup>a</sup> and Total Energies (au) Computed at the 4-31G Level

|                         | $(\Phi = 0^{\circ}, \theta = 60^{\circ})$ | $(\Phi=90^\circ, \theta=60^\circ)$ | $(\Phi=120^\circ,\theta=60^\circ)$ | $(\Phi=135^\circ, \theta=60^\circ)$ | $(\Phi=155^\circ,\theta=60^\circ)$ | $(\Phi = 180^\circ, \theta = 60^\circ)$ |
|-------------------------|---|------------------------------------|------------------------------------|-------------------------------------|------------------------------------|---|
| $r(0-C_2)$              | 1.3748                                    | 1.3935                             | 1.3885                             | 1.3863                              | 1.3840                             | 1.3830                                  |
| $\angle OC_2C_3$        | 128.69                                    | 123.55                             | 122.85                             | 122.77                              | 122.51                             | 122.32                                  |
| $\angle C_1 OC_2$       | 119.85                                    | 116.75                             | 116.20                             | 116.48                              | 117.19                             | 117.88                                  |
| Tilt angle <sup>b</sup> | -3.35c                                    | 1.62d                              | 1.56d                              | 1.48 <i>d</i>                       | 1.45 <i>d</i>                      | -3.31c                                  |
| Total energy            | -191.636 02                               | -191.62892                         | -191.63057                         | -191.631 21                         | -191.631 65                        | -191.632 08                             |

<sup>*a*</sup>Bond lengths in Å and angles in deg. <sup>*b*</sup> Tilt angle of the local threefold axis of the methyl group to the C-O bond. <sup>*c*</sup> Tilt angle optimized in the  $H_{c}C_{1}O$  plane. <sup>*d*</sup> Tilt angle optimized in the  $H_{a}C_{1}O$  plane.

Table III. Cisoid-Transoid Energy Differences and Methyl Rotational Barrier for Methyl Vinyl Ether

| Trans-<br>formation | Exptl, kcal/mol                 | STO-3G,<br>kcal/mol | 4-31G,<br>kcal/mol |
|---------------------|---------------------------------|---------------------|--------------------|
| TS-CS               | 1.15 ± 0.25 <i>a</i> , <i>b</i> | 0.96                | 2.47               |
| CE-TE               |                                 | 1.34                | -0.40              |
| CE-CS               | $3.83 \pm 0.1b$                 | 4.14                | 2.97               |
| TE-TS               |                                 | 1.84                | 0.89               |

<sup>a</sup> Experimental energy difference between the two isomers. <sup>b</sup> See ref 21b.

well with the experimental value, the agreement is poorer for the value computed at the 4-31G level.

Several aspects of the computational results listed in Tables I, II, and IV are of interest. (i) Recalling that the ethylenic C-C bond length computed with the same basis set is  $1.306 \text{ Å}^9$  we find that the corresponding C-C bond lengths in the various conformations of methyl vinyl ether are all larger than the ethylene value. (ii) The agreement between the values of the geometrical parameters computed at the minimal and extended levels is quite good, except for the  $\angle C_1OC_2$  angle, whose value increases significantly going from the STO-3G to the 4-31G basis set. However, this increase, 6-7°, is less than that of the  $\angle HOH$  angle in H<sub>2</sub>O for the same change of basis sets (10°).<sup>10</sup> (iii) The value of the O-C<sub>2</sub> bond length is not significantly altered during rotation.

A comment regarding the reliability of the basis set is necessary. Specifically, Pople and co-workers<sup>11</sup> have found that methyl rotation barriers are well reproduced by the basis sets used in our work. However, it is true that in cases involving a small barrier, like the CE-TE barrier, a basis set dependence may be manifested. It would be interesting to see how other good quality basis sets work in such cases.<sup>12</sup>

## Nonbonded Attractions in Methyl Vinyl Ether

In this section we shall trace the key factors dictating the unexpected conformational preference of methyl vinyl ether.

Since "steric effects" should favor a trans conformation, the comparative discussion will involve the CS and TS conformations. The analysis presented here is based on a qualitative MO approach and involves the following steps: (a) sequential dissection of the molecule under consideration into component fragments; (b) construction of the group MO's of each fragment by means of one-electron MO (OEMO) theory or explicit calculations; (c) examination of the key group orbital interactions which obtain in the course of the union of the component fragments to yield the composite system in a specified geometry.

In the course of our analysis, we shall make use of the following general results of one-electron MO theory.

(a) The interaction of a doubly occupied MO,  $\phi_i$ , with a vacant MO,  $\phi_j$ , leads to two-electron stabilization which is inversely proportional to the energy separation of the two MO's,  $E_i - E_j$ , and directly proportional to the square of their overlap integral,  $S_{ij}$ . This is a well-known result of

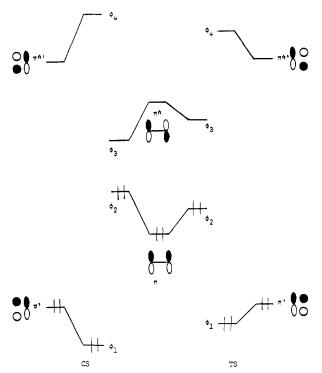


Figure 3. Interaction diagram of the  $B_a$  +  $B_b$  union in a CS and TS conformation.

perturbation theory<sup>13</sup> and the approximations involved in its derivation are valid for the systems studied in this work.<sup>14</sup> The algebraic expression for the two-electron stabilization is given below:

$$\Delta E_{ij}^{2} = S_{ij}^{2} (K - E_{i})^{2} / (E_{i} - E_{j})$$
(1)

(b) The interaction of two doubly occupied MO's,  $\phi_i$  and  $\phi_j$ , leads to net four-electron destabilization which increases as the overlap integral of the two MO's,  $S_{ij}$ , and the mean of their energies,  $(E_i + E_j)/2$ , increase.<sup>15</sup> This result is obtained by application of the variational method to the case of a two-orbital four-electron interaction and involves no additional assumptions other than the usual approximation of the interaction matrix element as a linear function of the overlap integral. The algebraic expression for the four-electron destabilization is given below:

$$\Delta E_{ij}^{4} = \frac{4S_{ij}^{2}}{1 - S_{ij}^{2}} (E_{0} - K)$$
<sup>(2)</sup>

where  $E_0$  is the mean of the energies of the  $\phi_i$  and  $\phi_j$  MO's before mixing.

Methyl vinyl ether can be dissected into fragments A and B. In turn, fragment B can be further dissected into the elementary fragments  $B_a$  and  $B_b$ , the wave functions of which are known. This kind of "theoretical surgery" is shown below.

We first proceed to construct the  $\pi$  MO's of fragment B from the  $\pi$  MO's of the methyl group (fragment B<sub>a</sub>) and the double bond (fragment B<sub>b</sub>). Figure 3 depicts the inter-

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|                         | CE                   |             | TE                         |             |  |
|-------------------------|----------------------|-------------|----------------------------|-------------|--|
|                         | STO-3G               | 4-31G       | STO-3G                     | 4-31G       |  |
| $r(C_1 - 0)$            | 1.4371               | (1.4371)    | 1.4431                     | (1.4431)    |  |
| $r(O-C_2)$              | 1.3924               | 1.3769      | 1.3950                     | 1.3811      |  |
| $r(C_2 - C_3)$          | 1.3148               | (1.3148)    | 1.3153                     | (1.3153)    |  |
| $\angle C_1 OC_2$       | 117.27               | 123.19      | 113.97                     | 119.94      |  |
| LOC,C,                  | 131.81               | 130.54      | 121.07                     | 122.26      |  |
| $\angle H_1 C_2 C_3$    | 121.63               | (121.63)    | 121.99                     | (121.99)    |  |
| $\angle C_2 C_3 H_2$    | 122.96               | (122.96)    | 121.26                     | (121.26)    |  |
| $\angle H_2C_3H_3$      | 115.49               | (115.49)    | 117.07                     | (117.07)    |  |
| Tilt angle <sup>b</sup> | -4.51                | -3.06       | -2.64                      | -1.86       |  |
| Total energy            | -189.489 68          | -191.631 29 | -189.491 81                | -191.630 65 |  |
| 0.                      | $(-191.628\ 68)^{c}$ |             | (-191.628 44) <sup>c</sup> |             |  |
| Nuclear energy          | 120.374 36           | 120.074 87  | 118.858 42                 | 118.546 35  |  |

| <sup>a</sup> Bond lengths in Å and bond angles in deg. <sup>b</sup> Tilt angle of the local threefold axis of the methyl group to the C–O bond computed in the |  |
|--|--|
| $H_cC_1O$ plane. <sup>c</sup> Energy value computed at the 4-31G level with the geometry optimized at the STO-3G level.  |  |

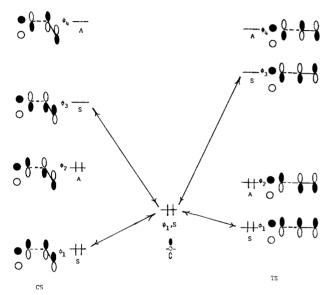
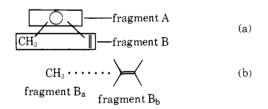


Figure 4. Interaction diagram of the A + B union for the CS and TS conformation of methyl vinyl ether. Arrows indicate the dominant orbital interactions. Symmetry labels refer to the pseudosymmetry of the  $B_a + B_b$  MO's.



actions between the  $\pi$  type MO's of the methyl group and the  $\pi$  MO's of the double bond. The key difference between the two conformations CS and TS is that in the former case the two 1s AO's of the methyl hydrogens H<sub>a</sub> and H<sub>b</sub> can overlap with the 2p<sub>z</sub> AO of the outer olefinic carbon, while in the latter case they cannot. On the basis of the general principles outlined before, we predict that the two-electron stabilization resulting from the  $\pi'-\pi^*$  and  $\pi-\pi^{*'}$  interactions will favor the TS conformation since the appropriate MO overlap integrals are greater for the TS than the CS conformer. Similarly, the four-electron destabilization arising from the  $\pi-\pi'$  interaction will also favor the TS conformation since  $S_{\pi\pi'}(CS) > S_{\pi\pi'}(TS)$ .

Once we have examined the energetics of the MO interactions which obtain in the course of the union of the  $\pi$  systems of the methyl group and the double bond, we return to

Table V.  $\pi$  Bond Orders of the CS and TS Conformations of Methyl Vinyl Ether

| Atom<br>pair          | Predicted $\pi$ bonding | $\pi$ bond orders (STO-3G) <sup>a</sup> |                    |  |  |
|-----------------------|-------------------------|---|--------------------|--|--|
|                       | in CS<br>relative to TS | CS<br>conformation                      | TS<br>conformation |  |  |
| $H_{ab}-C_1$          | _                       | 0.9628                                  | 0.9653             |  |  |
| H <sub>ab</sub> -O    | _                       | 0.3929                                  | 0.3998             |  |  |
| $H_{ab}^{ab} - C_2$   | _                       | -0.0583                                 | -0.0424            |  |  |
| $H_{ab}^{ab} - C_{3}$ | +                       | 0.1105                                  | 0.0932             |  |  |
| C <sub>1</sub> -O     | +                       | 0.0541                                  | 0.0447             |  |  |
| $C_1 - C_2$           | +                       | -0.0520                                 | -0.0377            |  |  |
| $C_1 - C_3$           | _                       | -0.0404                                 | -0.0333            |  |  |
| $\dot{O}-C_{2}$       | +                       | 0.1736                                  | 0.1485             |  |  |
| $O-C_3$               | _                       | -0.3731                                 | -0.3672            |  |  |
| $C_2 - C_3$           | _                       | 0.7655                                  | 0.7732             |  |  |

a Optimized geometries.

the interaction diagram of Figure 3 in order to make certain observations about the  $\pi$  MO's of fragment B. Specifically, it can be seen that, as a result of the orbital interaction pattern discussed before, the energies of the various  $\pi$  MO's of fragment B vary as follows, depending upon the geometry of union.

$$E_1(CS) < E_1(TS)$$
$$E_2(CS) > E_2(TS)$$
$$E_3(CS) < E_3(TS)$$
$$E_4(CS) > E_4(TS)$$

This pattern is not surprising to the theoretical organic chemist since it reflects nothing more than the fact that the CS conformation resembles an antiaromatic structure and the TS conformation a nonaromatic structure. The changes in the energies of the  $\pi$  MO's which accompany the TS  $\rightarrow$ CS transformation are characteristic of the changes in the energies of the  $\pi$  MO's accompanying nonaromatic  $\rightarrow$  antiaromatic transformation.

We are now prepared to consider the construction of the composite system of methyl vinyl ether from the  $\pi$  system of fragment B and the oxygen lone pair AO. The orbital interactions which obtain in this union are depicted in Figure 4. On the basis of the principles outlined before, we can determine that the  $\psi_1-\phi_3$  interaction is more destabilizing in the TS conformation. This four-electron destabilization which favors the CS conformation in the A + B union will more than compensate for the four-electron destabilization term which favors the TS conformation in the B<sub>a</sub> + B<sub>b</sub> union since we expect that the overlap integral  $S(\psi_1\phi_1)$  will

Table VI. *n*-Overlap Populations for the Various Conformations of Methyl Vinyl Ether

|                               | CS      |         | CE      |         | TS      |         | TE      |         |
|-------------------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| Atom pair                     | STO-3G  | 4-31G   | STO-3G  | 4-31G   | STO-3G  | 4-31G   | STO-3G  | 4-31G   |
| (1) $H_{ab}-C_1$              | 0.3667  | 0.3737  | 0.3689  | 0.3857  | 0.3677  | 0.3801  | 0.3684  | 0.3827  |
| (2) $H_{ab} = 0$              | -0.0119 | -0.0366 | -0.0128 | -0.0343 | -0.0119 | -0.0362 | -0.0127 | -0.0373 |
| $(3) H_{ab} - C_2$            | -0.0010 | 0.0013  | -0.0004 | -0.0008 | -0.0008 | 0.0014  | 0.0003  | 0.0000  |
| (4) $H_{ab} - C_3$            | 0.0014  | 0.0057  | 0.0001  | 0.0004  | 0.0001  | 0.0004  | 0.0000  | 0.0002  |
| $(5) C_1 - 0$                 | 0.0077  | -0.0029 | 0.0044  | -0.0182 | 0.0064  | -0.0048 | 0.0051  | -0.0101 |
| $(6) C_1 - C_2$               | -0.0016 | -0.0058 | -0.0008 | -0.0008 | -0.0011 | -0.0038 | -0.0008 | -0.0020 |
| $(7) C_1 - C_3$               | -0.0004 | -0.0018 | 0.0000  | 0.0008  | 0.0000  | -0.0003 | 0.0000  | 0.0000  |
| (8) O-C,                      | 0.0247  | 0.0077  | 0.0248  | 0.0037  | 0.0211  | -0.0044 | 0.0218  | -0.0042 |
| $(9) O - C_3$                 | -0.0039 | -0.0177 | -0.0037 | -0.0179 | -0.0048 | -0.0197 | -0.0049 | -0.0207 |
| $(10) C_2 - C_3$              | 0.1899  | 0.2526  | 0.1897  | 0.2535  | 0.1915  | 0.2577  | 0.1909  | 0.2573  |
| Total π-overlap<br>population | 0.5716  | 0.5803  | 0.5702  | 0.5721  | 0.5682  | 0.5704  | 0.5675  | 0.5659  |

be much larger in the case of A + B union relative to the  $S(\pi\pi')$  overlap integral in the  $B_a + B_b$  union. Furthermore, the two-electron stabilizing term which favors the TS conformation in the  $B_a + B_b$  union will be dominated by the two-electron stabilizing term which favors the CS conformation in the A + B union because of a larger MO overlap integral and a smaller energy difference between the interacting orbitals. In general, the four-electron destabilization of the first union favoring the least crowded structure will tend to be counteracted by the four-electron destabilization of the second union which favors the more crowded structure. As a result, the relative two-electron stabilization which is greater in the second union than in the first union will favor a greater overall stabilization of the more crowded structure.

The previous analysis focused upon the energetics of changes which accompany the union of two fragments in a specified geometry, i.e., it was an "energy approach". Further insights are gained by adopting a "charge transfer approach". In this case, conceptual simplicity can be achieved by using perturbation theory with neglect of overlap. This approach and the principles involved have been discussed in our previous work.<sup>3a</sup>

Neglect of overlap will automatically eliminate the effects of four-electron repulsive interactions upon bonding. However, we have already seen that overlap repulsion may favor the more "crowded" conformer relative to a "uncrowded" geometry. Hence, one does not lose essential information by neglecting overlap in the "charge transfer approach".

In the "charge transfer" approach, we are concerned with the bonding changes which occur in the two conformations, CS and TS, as a result of the  $\psi_1 - \phi_3$  stabilizing interaction which gives rise to charge transfer from  $\psi_1$  to  $\phi_3$ . From the nodal properties of  $\phi_3$ , it can be seen that charge transfer will increase bonding between the 1s AO's of Ha and  $H_b$  and the  $2p_z$  AO of the outer carbon. Furthermore, the increase in the  $H_{a,b}(1s)-C_3(2p_z)$  bond order will be greater for the CS than the TS conformation because the  $O(2p_z)-\phi_3$  interaction is stronger in the former case. In addition, orbital overlap between the AO's is appreciable in the CS and zero in the TS conformation, e.g., the positive  $H_{a,b}(1s)-C_3(2p_z)$  bond order is felt only in the CS conformation. Hence, we can say that there is an attractive nonbonded 1,5 interaction which favors the CS over the TS conformation.

A further examination of the consequences of charge transfer by means of the interaction diagram of Figure 4 leads to clear-cut predictions about the relative magnitude of  $\pi$  bonding between any pair of atoms in the CS and TS conformations. Recalling that the  $O(2p_z)-\phi_3$  interaction is stronger and leads to greater charge transfer in the CS conformation, one can predict whether a certain  $\pi$  interaction between any pair of atoms will be more bonding or antibonding in the CS conformation relative to the TS conformation. These predictions are given in Table V along with the corresponding  $\pi$  bond orders calculated at the STO-3G level. It can be seen that the consequences of charge transfer in the relative  $\pi$  bonding of the CS and TS conformations, as predicted by our orbital symmetry approach, are confirmed by the ab-initio calculations. Specifically, the percentage of correct predictions is 90%! The  $\pi$ -overlap population for atom pairs as well as the total  $\pi$ -overlap population for a particular conformation are shown in Table VI. Keeping in mind the predictions shown in Table V, we see from Table VI that the percentage of correct predictions concerning the relative  $\pi$  bonding in the CS and TS conformations is 70%. However, the discrepancies are small and can be understood by reference to the fact that the predictions were based upon a rigid rotor model while the ab-initio calculations refer to geometry optimized structures. For example, the  $\pi$  bond order O-C<sub>3</sub> was correctly predicted by our approach while the O-C<sub>3</sub>  $\pi$  overlap population was not. This disagreement arises in the smaller  $C_1OC_2$  and  $OC_2C_3$ angles in the TS relative to the CS conformation which force a larger O-C<sub>3</sub>  $\pi$  overlap. We also see from Table VI that the total  $\pi$  overlap population (STO-3G) is greater for the CS than for the TS conformation. This result is paralleled by the total energies calculated at the STO-3G level and is in accord with our theoretical analysis which attributes the lower energy of the CS conformation relative to the TS conformation to  $\pi$  interactions.

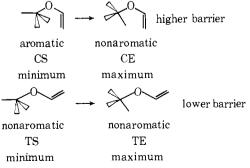
We now turn to a comparison of the  $\pi$  overlap populations computed at the STO-3G and 4-31G levels. The correlation between the predicted relative  $\pi$  bonding in the conformations CS and TS and the calculated  $\pi$  overlap populations is, as in the STO-3G calculation, quite good for the 4-31G calculation with the percentage of correct predictions being 80%. In the interconversions  $CS \rightarrow TS$ ,  $CE \rightarrow$ TE, CS  $\rightarrow$  CE, and TS  $\rightarrow$  TE we find, with both basis sets, a decrease in the total  $\pi$  overlap population when the interconversion involves a decrease in nonbonded attraction. It is important to point out that when the basis set is changed from STO-3G to 4-31G the magnitude of the long-range  $\pi$ -overlap population, H<sub>a,b</sub>-C<sub>3</sub>, increases. That is, an improvement in the quality of the basis set results in an increase in nonbonded attraction as reflected in the Ha,b-C3  $\pi$ -overlap population. This increase is largest in the CS conformation in which nonbonded attraction is the largest.

In summary, a MO analysis of the relative  $\pi$  energies of the CS and TS conformations leads to the prediction that the former will be more stable, a preference which can be attributed to a nonbonded attractive interaction between the methyl group and the double bond. Once more, we em-

phasize that the term nonbonded attraction denotes a stabilizing effect brought about by virtue of having two atoms or groups in proximity to each other. A similar approach can be used for comparing the stabilization of the CE and TE conformations relative to that of the CS conformation. Since appreciable  $H_{ab}$ -C<sub>3</sub>  $\pi$ -bonding overlap obtains only in the CS conformation, we would expect this conformation to have lower energy than either the CE or TE conformation. This expectation is confirmed by the ab initio calculations as can be seen in comparing the results contained in Tables I, II, and IV. Also, the total  $\pi$ -overlap population (Table VI) is larger for the CS than the CE and TE conformations. In short, there is excellent agreement between the qualitative predictions of the OEMO model and the ab-initio results. This state of affairs has, in fact, led us to seek additional "reasons" for the success of the OEMO model and we hope to report on that at a later date. The second important result of the ab-initio calculations concerns the relative magnitude of the methyl rotational barrier in the cisoid and transoid conformations. These values are listed in Table III. Once more, the MO analysis outlined before can be effectively utilized to interpret these interesting results. The barrier in the cisoid geometry will correspond to the energy difference between the CS and CE conformations with the CS conformation being an energy minimum and the CE conformation being an energy maximum. On the other hand, the barrier in the transoid geometry will correspond to the energy difference between the TS and the TE conformation with the TS conformation being the energy minimum and the TE conformation the energy maximum. It is immediately obvious that rotation of the methyl group in the cisoid geometry will be unfavorable relative to that in the transoid geometry because in the former case an  $H_{a,b}$ -C<sub>3</sub> attractive interaction is destroyed in the process while such a destructive effect is absent in the transoid geometry. In other words, we expect that the energy minimum CS will be more stable than the energy minimum TS and the two energy maxima CE and TE will be comparable in energy.

A simplifying reduction of the above detailed analysis of the conformational properties of methyl vinyl ether can be accomplished by recourse to the concept of aromaticity shown to be directly applicable to problems of geometrical and conformational isomerism.<sup>5</sup> Specifically, methyl vinyl ether is a  $6\pi$ -electron system and, thus, the preferred conformation is predicted to be the CS conformation which corresponds to a Hückel aromatic system.

Furthermore, the relative magnitude of the rotational barriers and energy differences between cisoid and transoid conformation can be predicted by considering the aromatic, nonaromatic, or antiaromatic character of the minima and maxima of the rotational curve. These predictions are outlined below:

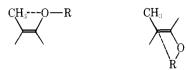


The computed rotational barriers listed in Table III are in full accord with these predictions.

The results of this work have a direct bearing on the question of the conformational control of the relative stability of geometric isomers. For example, Okuvama et al.<sup>16</sup> have studied the relative stability of pairs of cis and trans  $\alpha,\beta$ -unsaturated ethers, such as the ones shown below:



It was found that when R is isopropyl or tert-butyl, the cis isomer is more stable, while when R is methyl or isobutyl, the reverse situation obtains. Now, a CH3-OR attractive nonbonded interaction will obtain in the cis isomer and an  $R-C_1$  attractive nonbonded interaction will be possible only in the trans isomer simply because of steric reasons. In other words, when R is a "small" alkyl group, one compares the following two structures:



Nonbonded attraction obtains in both geometric isomers and the greater stability of the trans isomer can be taken as a measure of the relative strength of the two different kinds of attractive nonbonded interactions. On the other hand, when R is a "bulky" alkyl group, one compares the following two structures:



Nonbonded attraction obtains only in the cis isomer which is found to be more stable than the trans isomer.

In closing, we can say that the concept of nonbonded attraction leads to many detailed electronic predictions which are supported by ab-initio calculation.<sup>17</sup>

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